

Domain Specific Languages to Tame Heterogeneous and Emerging Computing Systems

Jeronimo Castrillon

Chair for Compiler Construction (CCC)

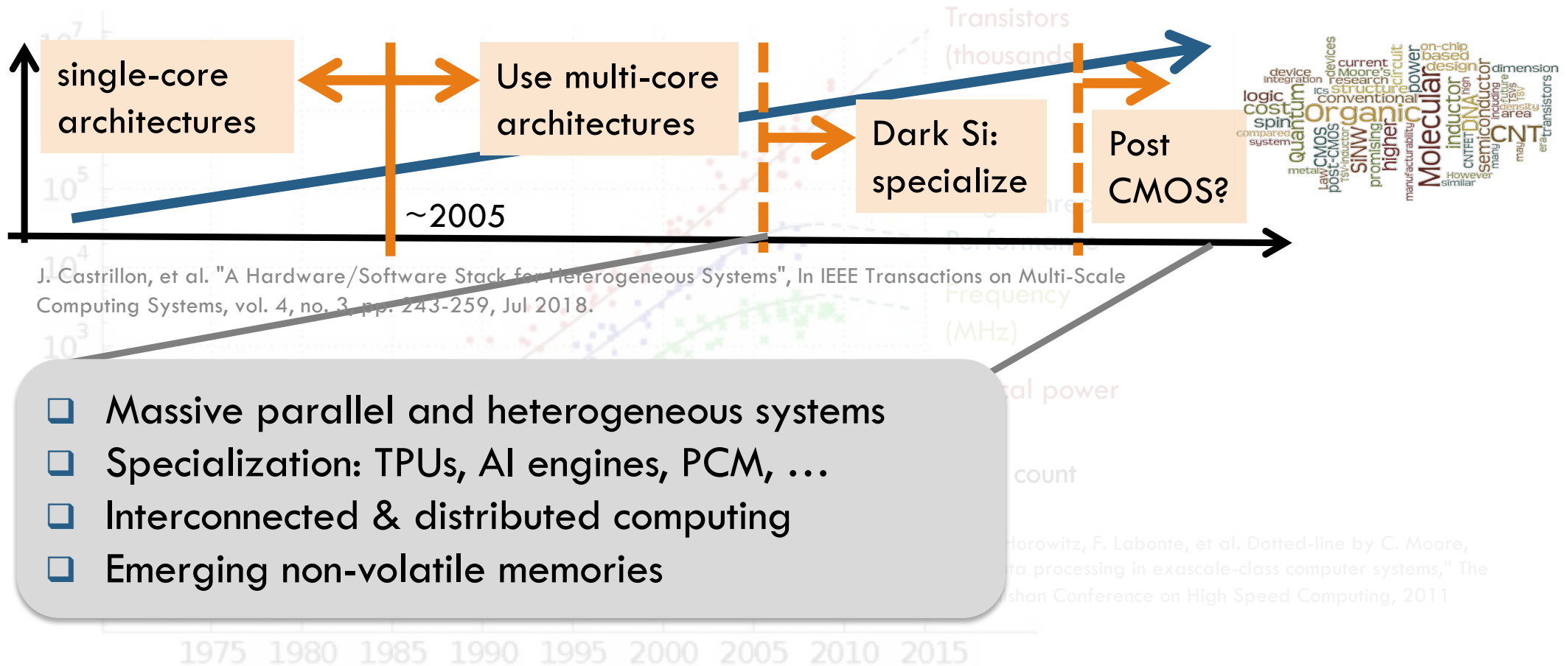
TU Dresden, Germany

The Platform for Advanced Scientific Computing (PASC) Conference

Geneva (virtual), Switzerland

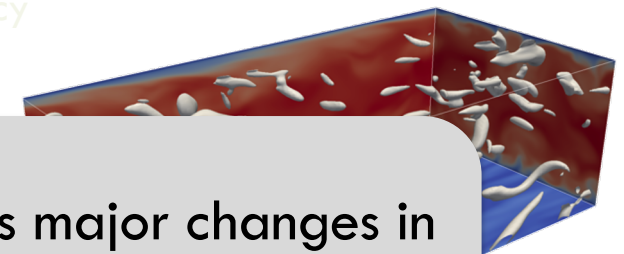
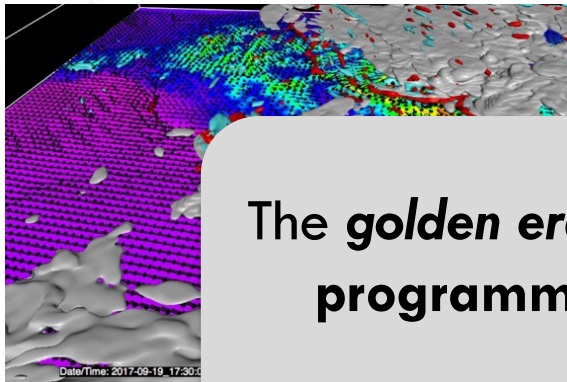
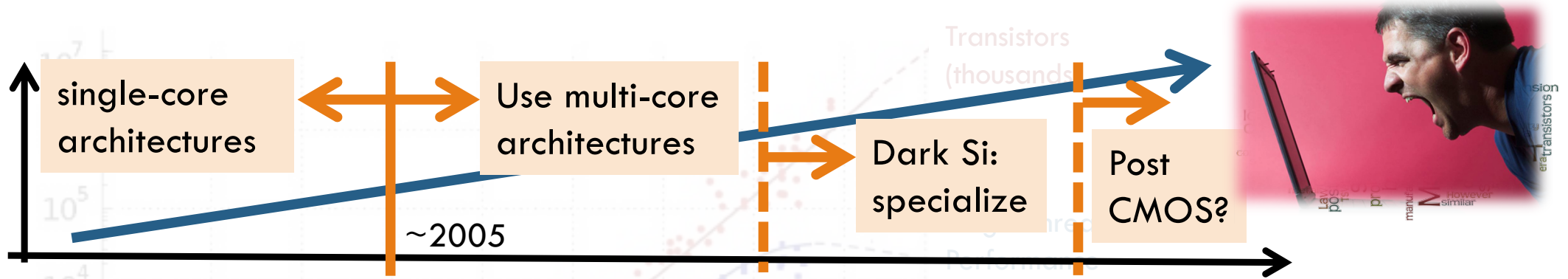
July 9, 2021

Evolution of computing



- Massive parallel and heterogeneous systems
- Specialization: TPUs, AI engines, PCM, ...
- Interconnected & distributed computing
- Emerging non-volatile memories

Evolution of computing: Programming



The **golden era** in computer architecture requires major changes in **programming methods** to **democratize** heterogeneous and emerging high-performance computing

What's wrong with good old sequential languages?

$$v_{ijk,e} = \sum_{i'=0}^p \sum_{j'=0}^p \sum_{k'=0}^p A_{kk'} A_{jj'} A_{ii'} u_{i'j'k'} e$$

What we want

What we (naively) code

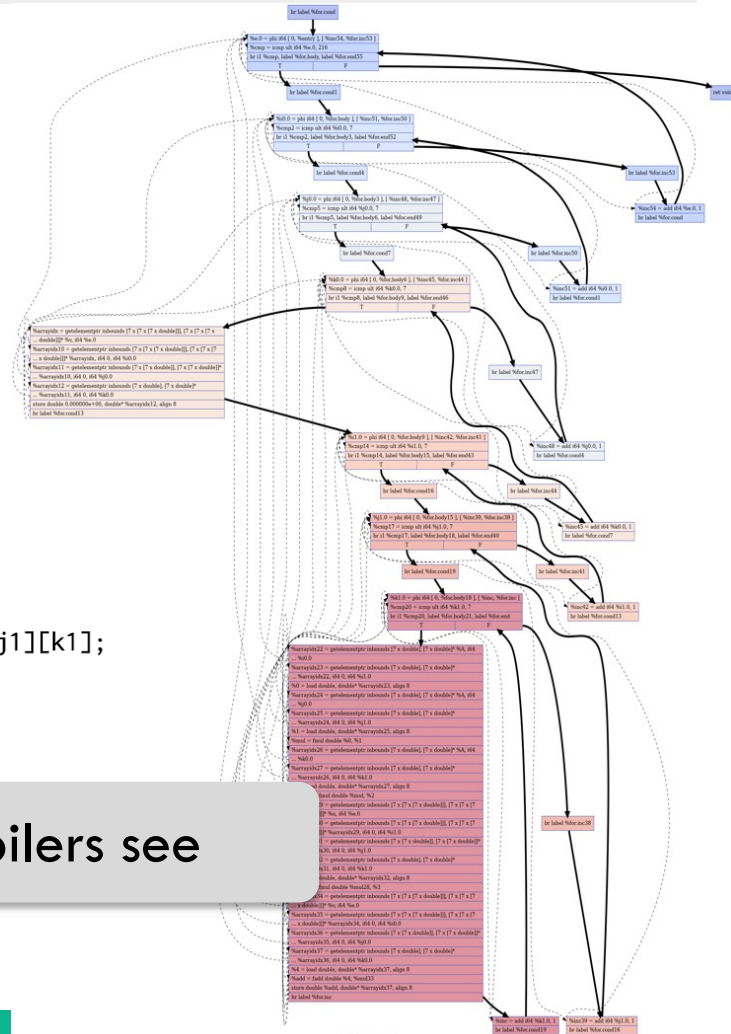
```

1 void cfd_kernel(
2   double A[restrict] 7][7],
3   double u[restrict] 216][7][7][7],
4   double v[restrict] 216][7][7][7])
5 {
6   /* element loop: */
7   for(int e = 0; e < 216; e++) {
8     for(int i0 = 0; i0 < 7; i0++) {
9       for(int j0 = 0; j0 < 7; j0++) {
10        for(int k0 = 0; k0 < 7; k0++) {
11          v[e][i0][j0][k0] = 0.0;
12          for(int i1 = 0; i1 < 7; i1++) {
13            for(int j1 = 0; j1 < 7; j1++) {
14              for(int k1 = 0; k1 < 7; k1++) {
15                v[e][i0][j0][k0] += A[i0][i1]
16                  * A[j0][j1]
17                  * A[k0][k1]
18                  * u[e][i1][j1][k1];
19              } } } } }
20          } /* end of element loop */
21        }
22      }
23    }
24  }

```

How many more times should we optimize this manually?

What compilers see



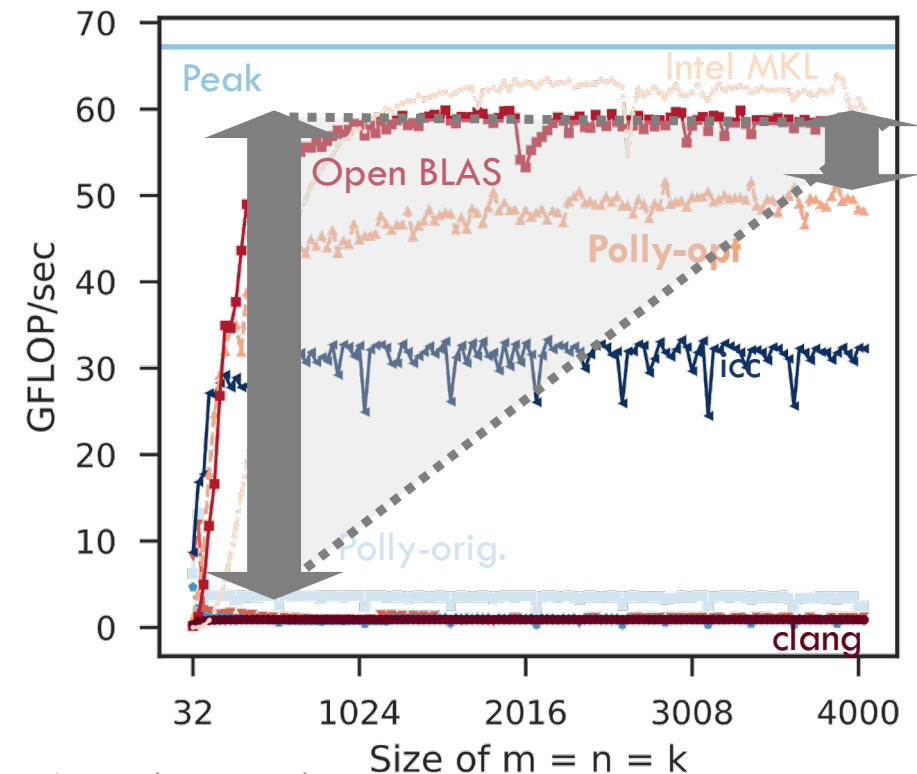
Polyhedral compilation: Hope for regular loops

- Recognize high-level patterns like **matrix multiply-and-add operation (MMA)**

“Our method attained the performance of vendor optimized BLAS libraries”

Complex and sensitive **pattern recognition** to help close the performance gap

Intel Kaby Lake



R. Gareev, T. Grosser, M. Kruse. "High-performance generalized tensor operations: A compiler-oriented approach." ACM Transactions on Architecture and Code Optimization (TACO) 15.3 (2018): 34.

There is only so much we can do/reconstruct...

- Lots of progress: polyhedral compilers, trace-driven dynamic parallelization, patterns/idiom extraction

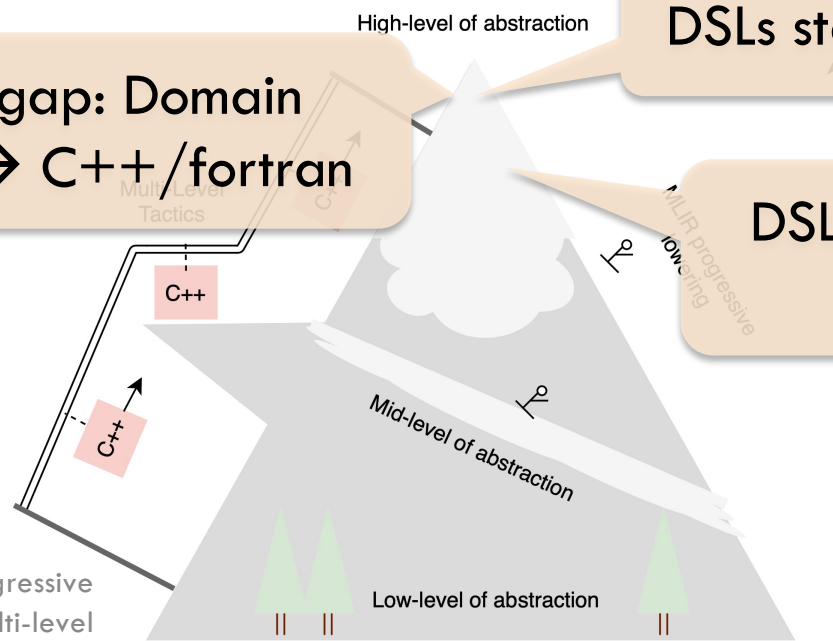
```

19 while(!queue.empty())
20 {
21     // Dequeue a vertex from queue
22     s = queue.front();
23     queue.pop_front();
24
25     // Apply function f to s, accumulate values
26     result += f(s);
27
28     // Get all adjacent vertices of s.
29     // If an adjacent node hasn't been visited,
30     // then mark it as visited and enqueue it
31     for(i=adj[s].begin(); i!=adj[s].end(); ++i)
32         f(*i);
33     queue.push_back(*i);
34 }
35 }
36 }
37 }
38 }
39 }
40
41 return result;
42 }
    
```

Bridge gap: Domain experts → C++/fortran

DSLs start here!

DSLs for performance: Halide, Spiral, TVM, TensorFlow, Firedrake...



L. Chelini, et al. "Progressive Raising in Multi-level IR." CGO 2021

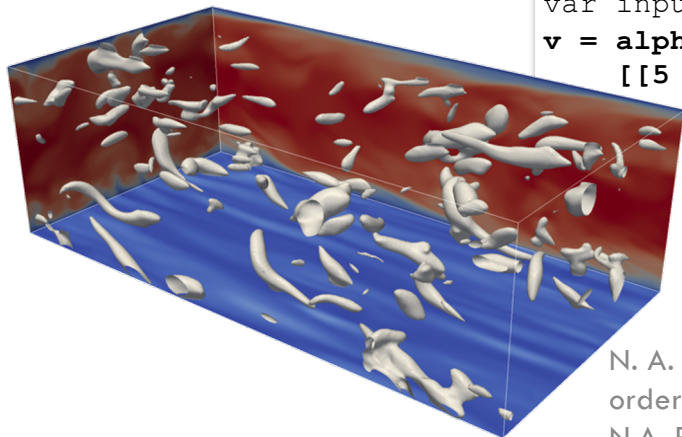
S. Manilov, C. Vasiladiotis, B. Franke. "Generalized profile-guided iterator recognition." CC 2018.

Examples (1): Tensors expressions (CFD, ML)

- ❑ Expression-language for tensor operations and optimizations
 - ❑ Originally for spectral element methods in computational fluid dynamics

$$\mathbf{v}_e = (\mathbf{A} \otimes \mathbf{A} \otimes \mathbf{A}) \mathbf{u}_e$$

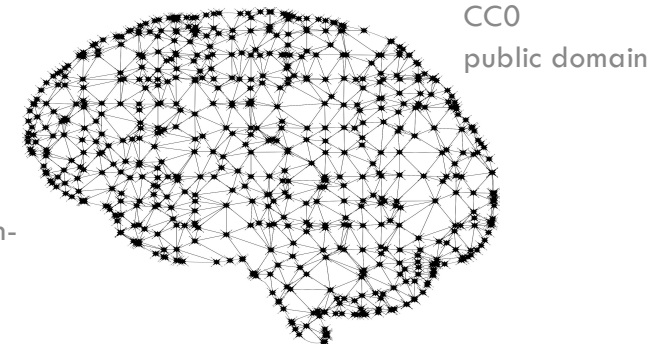
Interpolation kernel



```
source = ...
var input A : matrix &
var input u : tensorIN &
var input output v : tensorOUT &
var input alpha : [] &
var input beta : [] &
v = alpha * (A # A # A # u .
[[5 8] [3 7] [1 6]]) + beta * v
```

```
auto A = Matrix(m, n), B = Matrix(m, n),
      C = Matrix(m, n);
auto u = Tensor<3>(n, n, n);
auto v = (A*B*C)(u);
```

Fortran and C++ integration



N. A. Rink, et al. "CFDlang: High-level code generation for high-order methods in fluid dynamics". RWDSL'18.

N.A. Rink, N. A. and J. Castrillon. "Tell: a type-safe imperative Tensor Intermediate Language", ARRAY'19, pp. 57-68

Semantic gap → performance gap

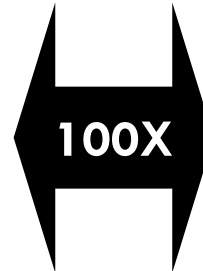
```
source = ...
var input A : matrix &
var input u : tensorIN &
var input output v : tensorOUT &
var input alpha : [] &
var input beta : [] &
v = alpha * (A # A # A # u .
  [[5 8] [3 7] [1 6]]) + beta * v
```

$$v_e = (A \otimes A \otimes A) u_e$$

$$v_{ijk,e} = \sum_{i'=0}^p \sum_{j'=0}^p \sum_{k'=0}^p A_{kk'} A_{jj'} A_{ii'} u_{i'j'k'e}$$

What we (naively) code

```
1 void cfd_kernel(
2   double A[restrict 7][7],
3   double u[restrict 216][7][7][7],
4   double v[restrict 216][7][7][7])
5 {
6   /* element loop: */
7   for(int e = 0; e < 216; e++) {
8     for(int i0 = 0; i0 < 7; i0++) {
9       for(int j0 = 0; j0 < 7; j0++) {
10        for(int k0 = 0; k0 < 7; k0++) {
11          v[e][i0][j0][k0] = 0.0;
12          for(int i1 = 0; i1 < 7; i1++) {
13            for(int j1 = 0; j1 < 7; j1++) {
14              for(int k1 = 0; k1 < 7; k1++) {
15                v[e][i0][j0][k0] += A[i0][i1]
16                                     * A[j0][j1]
17                                     * A[k0][k1]
18                                     * u[e][i1][j1][k1];
19              } } } } }
20          } } } } }
21        } } } } }
22      } } } } }
23    } } } } }
24  } } } } }
25 } /* end of element loop */
26 }
```



```
1 void cfd_kernel(
2   double A[restrict 7][7],
3   double u[restrict 216][7][7][7],
4   double v[restrict 216][7][7][7])
5 {
6   /* element loop: */
7   #pragma omp for
8   for (int e = 0; e < 216; e++) {
9     double t6[7][7][7];
10    /* 1st contraction: */
11    #pragma simd
12    for (int i0 = 0; i0 < 7; i0++) {
13      for (int i1 = 0; i1 < 7; i1++) {
14        /* #pragma simd */
15        for (int i2 = 0; i2 < 7; i2++) {
16          double t8 = 0.0;
17          for (int i3 = 0; i3 < 7; i3++)
18            t8 += A[i0][i3] * u[e][i1][i2][i3];
19          t6[i0][i1][i2] = t8;
20        } } } /* end of 1st contraction */
21    double t7[7][7][7];
22    /* 2nd contraction: */
23    #pragma simd
24    for (int i4 = 0; i4 < 7; i4++) {
25      for (int i5 = 0; i5 < 7; i5++) {
26        /* #pragma simd */
27        for (int i6 = 0; i6 < 7; i6++) {
28          double t9 = 0.0;
29          for (int i7 = 0; i7 < 7; i7++)
30            t9 += A[i4][i7] * t6[i5][i6][i7];
31          t7[i4][i5][i6] = t9;
32        } } } /* end of 2nd contraction */
33    /* 3rd contraction: */
34    #pragma simd
35    for (int i8 = 0; i8 < 7; i8++) {
36      for (int i9 = 0; i9 < 7; i9++) {
37        /* #pragma simd */
38        for (int i10 = 0; i10 < 7; i10++) {
39          double t10 = 0.0;
40          for (int i11 = 0; i11 < 7; i11++)
41            t10 += A[i8][i11] * t7[i9][i10][i11];
42          v[e][i8][i9][i10] = t10;
43        } } } /* end of third contraction */
44      } } } /* end of element loop */
45    }
```

What performance experts code

Closing the performance gap

- ❑ Not really optimization magic
 - ❑ Leverage expert knowledge
 - ❑ Algebraic identities

$$v_{ijk} = \sum_{l,m,n} (A_{kn} \cdot (A_{jm} \cdot (A_{il} \cdot u_{lmn})))$$

$$v_{ijk} = \sum_{l,m,n} (A_{kn} \cdot A_{jm}) \cdot (A_{il} \cdot u_{lmn})$$

$$v_{ijk} = \sum_{l,m,n} (A_{kn} \cdot ((A_{jm} \cdot A_{il}) \cdot u_{lmn}))$$

N. A. Rink, et al. "CFDlang: High-level code generation for high-order methods in fluid dynamics". RWDSL'18.

A. Susungi, et al., "Towards Compositional and Generative Tensor Optimizations", GPCE'17 pp. 169–175.

Easy to generate,
hard to transform

Actual code variants

Closing the performance gap

Not really optimization magic

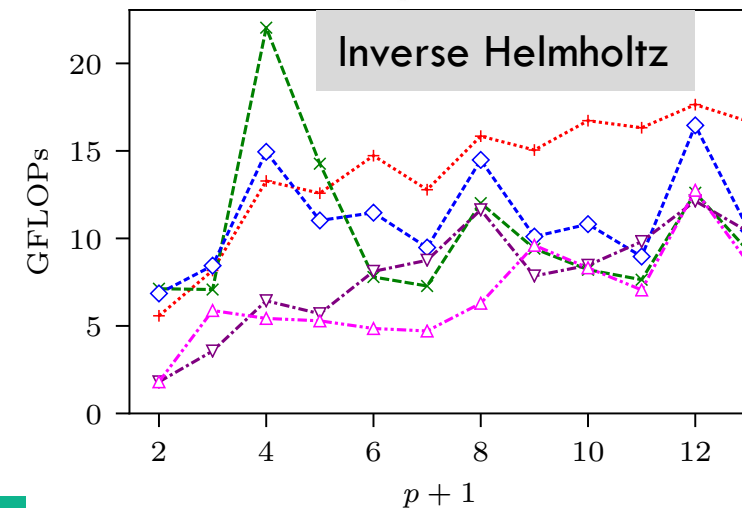
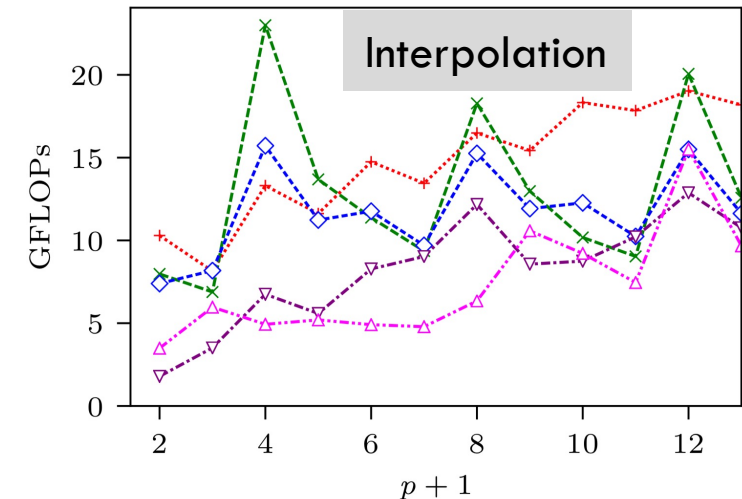
- ❑ Leverage expert knowledge
- ❑ Algebraic identities

$$v_{ijk} = \sum_{l,m,n} (A_{kn} \cdot (A_{jm} \cdot (A_{il} \cdot u_{lmn})))$$

$$v_{ijk} = \sum_{l,m,n} (A_{kn} \cdot A_{jm}) \cdot (A_{il} \cdot u_{lmn})$$

$$v_{ijk} = \sum_{l,m,n} (A_{kn} \cdot ((A_{jm} \cdot A_{il}) \cdot u_{lmn}))$$

- +...+ CFDlang(outer)
- *--* CFDlang(inner)
- ◇--◇ hand-optimized
- ▽--▽ DGEMM
- △--△ specialized



N. A. Rink, et al. "CFDlang: High-level code generation for high-order methods in fluid dynamics". RWDSL'18.

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TeML: Meta-programming for tensor optimizations

- Generalize for cross-domain tensor expressions
- Formal semantics and composition of transformations

$$\begin{aligned} \mathcal{E}_l[\text{stripmine}(l, r, v)] &= \\ &\lambda\sigma.\text{let } \langle i_1, \dots, \langle i_r, xs \rangle \dots \rangle = \sigma(l) \\ &\quad (b, e, 1) = i_r \\ &\quad i'_r = (0, (e - b)/v - 1, 1) \\ &\quad i'_{r+1} = (b + v \cdot i'_r, b + v \cdot i'_r + (v - 1), 1) \\ &\text{in } \langle i_1, \dots, \langle i'_r, [\langle i'_{r+1}, xs \rangle] \rangle \dots \rangle \\ \mathcal{E}_l[\text{interchange}(l, r_1, r_2)] &= \\ &\lambda\sigma.\text{let } \langle i_1, \dots, \langle i_{r_1}, \dots, \langle i_{r_2}, xs \rangle \dots \rangle \dots \rangle = \sigma(l) \\ &\text{in } \langle i_1, \dots, \langle i_{r_2}, \dots, \langle i_{r_1}, xs \rangle \dots \rangle \dots \rangle \end{aligned}$$

Formally defined transformation primitives

$$\mathcal{P}_{\text{stmt}}[\text{tile}(l, v)] = \mathcal{P}_{\text{prog}} \left[\begin{array}{l} l_0 = \text{stripmine_n}(l, d, v) \\ l_1 = \text{interchange_n}(l_0, 2, 2d - 2) \\ l_2 = \text{interchange_n}(l_1, 3, 2d - 3) \\ \dots \\ l_{d-1} = \text{interchange_n}(l_{d-2}, d, d) \\ l' = \text{interchange_n}(l_{d-1}, d + 1, d - 1) \end{array} \right]$$

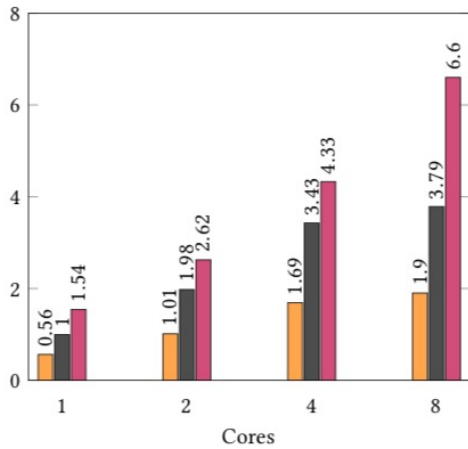
Higher-level transformations via composition

| | |
|--------------------------------------|---|
| $\langle \text{program} \rangle$ | $::= \langle \text{stmt} \rangle \langle \text{program} \rangle$ ϵ |
| $\langle \text{stmt} \rangle$ | $::= \langle id \rangle = \langle \text{expression} \rangle$ $\langle id \rangle = \Theta(\langle id \rangle : \langle \text{expression} \rangle)$ codegen ($\langle ids \rangle$) init (...) |
| $\langle \text{expression} \rangle$ | $::= \langle \text{Texpression} \rangle$ $\langle \text{Lexpression} \rangle$ |
| $\langle \text{Texpression} \rangle$ | $::= \text{scalar } ()$ tensor ($[\langle ints \rangle]$) eq ($\langle id \rangle, \langle iters \rangle? \rightarrow \langle iters \rangle$) vop ($\langle id \rangle, \langle id \rangle, [\langle iters \rangle?, \langle iters \rangle?]$) op ($\langle id \rangle, \langle id \rangle, [\langle iters \rangle?, \langle iters \rangle?] \rightarrow \langle iters \rangle$) |
| $\langle \text{Lexpression} \rangle$ | $::= \text{build } (\langle id \rangle)$ stripmine ($\langle id \rangle, \langle int \rangle, \langle int \rangle$) interchange ($\langle id \rangle, \langle int \rangle, \langle int \rangle$) fuse_outer ($\langle id \rangle, \langle id \rangle, \langle int \rangle$) fuse_inner ($\langle id \rangle, \langle int \rangle$) unroll ($\langle id \rangle, \langle int \rangle$) |
| $\langle iters \rangle$ | $::= [\langle ids \rangle]$ |
| $\langle id \rangle$ | $::= \langle id \rangle (, \langle id \rangle)^*$ |
| $\langle ints \rangle$ | $::= \langle int \rangle (, \langle int \rangle)^*$ |

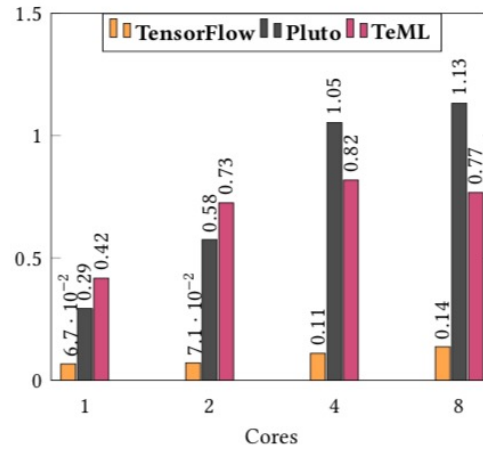
A. Susungi, et al. "Meta-programming for cross-domain tensor optimizations" GPCE'18, 79-92

Meta-programming for optimizations: Results

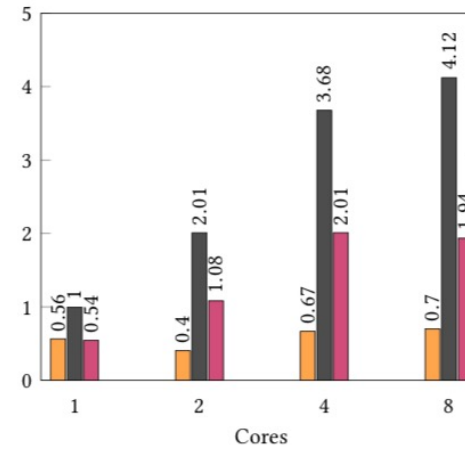
(a) mttkrp



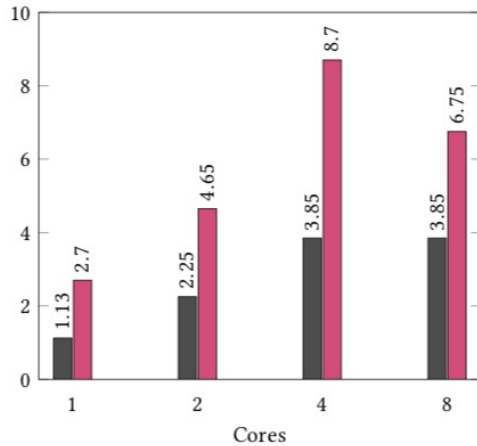
(b) bmm



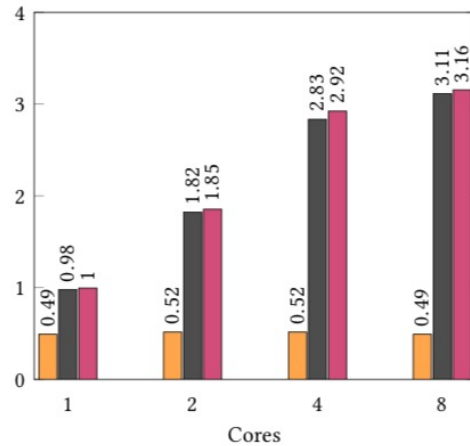
(c) sddmm



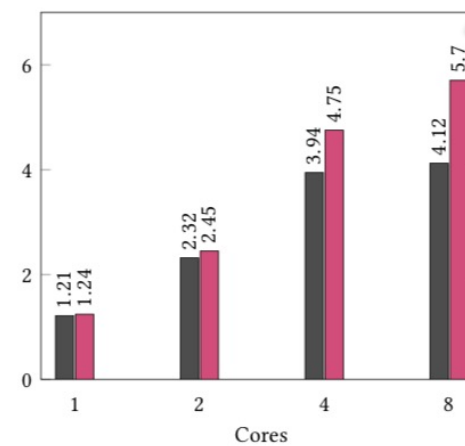
(d) gconv



(e) interp



(f) helm



Performance of Pluto could be reproduced

Higher abstraction → more optimization potential

A. Susungi, et al. "Meta-programming for cross-domain tensor optimizations", GPCE'18, 79-92

Tell: Formal language – added value

- ❑ Core common to multiple tensor languages
- ❑ Index-free notation and strong type system
- ❑ **Provably** no out-of-bound accesses

```
A = placeholder((m,h), name='A')
B = placeholder(h,h), name='B')
k = reduce_axis(0, h, name='k')
C = compute((m,k=1, lambda i, j:
            sum(A[k, i] * B[k, j], axis=k))
```

$\llbracket \cdot \rrbracket : \text{Context} \rightarrow \text{Memory} \rightarrow (\text{list of Nat}) \rightarrow \mathbb{D}$

$\llbracket x \rrbracket \Gamma \mu \bar{i} = \mu x \bar{i}$

$\llbracket (e) \rrbracket \Gamma \mu \bar{i} = \llbracket e \rrbracket \Gamma \mu \bar{i}$

$\llbracket \text{add } e_0 e_1 \rrbracket \Gamma \mu \bar{i} = \llbracket e_0 \rrbracket \Gamma \mu \bar{i} + \llbracket e_1 \rrbracket \Gamma \mu \bar{i}$

$\llbracket \text{mul } e_0 e_1 \rrbracket \Gamma \mu \bar{i} = \begin{cases} \llbracket e_0 \rrbracket \Gamma \mu [] \cdot \llbracket e_1 \rrbracket \Gamma \mu \bar{i}, & \text{if } \text{type}_{\Gamma}(e_0) = [] \\ \llbracket e_0 \rrbracket \Gamma \mu \bar{i} \cdot \llbracket e_1 \rrbracket \Gamma \mu \bar{i}, & \text{otherwise} \end{cases}$

$\llbracket \text{prod } e_0 e_1 \rrbracket \Gamma \mu (\bar{i}_0 \# \bar{i}_1) = \llbracket e_0 \rrbracket \Gamma \mu \bar{i}_0 \cdot \llbracket e_1 \rrbracket \Gamma \mu \bar{i}_1,$
if $\text{rank}_{\Gamma}(e_0) = \text{length}(\bar{i}_0)$ and $\text{rank}_{\Gamma}(e_1) = \text{length}(\bar{i}_1)$

$\llbracket \text{red}_+ i e \rrbracket \Gamma \mu [j_1, \dots, j_{i-1}, j_i, \dots, j_k] = \sum_{m=1}^n \llbracket e \rrbracket \Gamma \mu [j_1, \dots, j_{i-1}, m, j_i, \dots, j_k],$ if $\text{type}_{\Gamma}(e) = [n_1, \dots, n_{i-1}, n, n_{i+1}, \dots, n_{k+1}]$

N.A. Rink, N. A. and J. Castrillon. "Tell: a type-safe imperative Tensor Intermediate Language", ARRAY'19, pp. 57-68

$\llbracket \text{transp } i_0 i_1 e \rrbracket \Gamma \mu [j_1, \dots, j_{i_0}, \dots, j_{i_1}, \dots, j_k] =$

$\llbracket e \rrbracket \Gamma \mu [j_1, \dots, j_{i_1}, \dots, j_{i_0}, \dots, j_k]$

$\llbracket \text{diag } i_0 i_1 e \rrbracket \Gamma \mu [j_1, \dots, j_{i_0-1}, j_{i_0}, j_{i_0+1}, \dots, j_{i_1-1}, j_{i_1}, \dots, j_k] =$

$\llbracket e \rrbracket \Gamma \mu [j_1, \dots, j_{i_0-1}, j_{i_0}, j_{i_0+1}, \dots, j_{i_1-1}, j_{i_1}, j_{i_1+1}, \dots, j_k]$

$\llbracket \text{expa } i n e \rrbracket \Gamma \mu [j_1, \dots, j_{i-1}, j_i, j_{i+1}, \dots, j_k] =$

$\llbracket e \rrbracket \Gamma \mu [j_1, \dots, j_{i-1}, j_{i+1}, \dots, j_k]$

$\llbracket \text{proj } i m e \rrbracket \Gamma \mu [j_1, \dots, j_{i-1}, j_i, \dots, j_k] =$

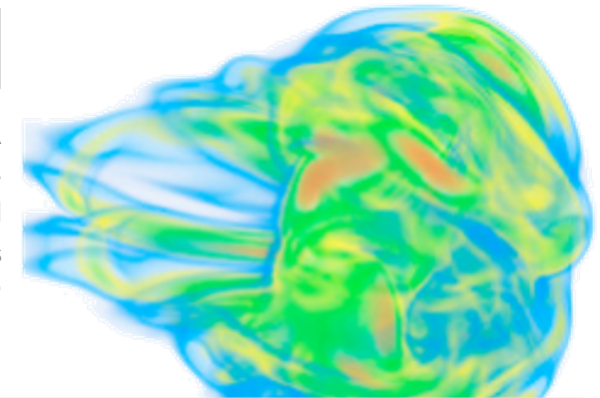
$\llbracket e \rrbracket \Gamma \mu [j_1, \dots, j_{i-1}, m, j_i, \dots, j_k]$

Examples (2): Particle-mesh simulations

- ❑ Particle-mesh simulations in computational biology
 - ❑ Discrete/continuous
 - ❑ Deterministic/stochastic

Vortex ring

P. Incardona, et al "OpenFPM: A scalable open framework for particle and particle-mesh codes on parallel computers", Computer Physics Communications, 2019



time loop

start: 0 stop: 1000

temporal method: explicit_euler

spatial method: DG-PSE

$$\frac{\partial u}{\partial t} = Du * \nabla^2 u - u * v^2 + F * (1 - u)$$

$$\frac{\partial v}{\partial t} = Dv * \nabla^2 v + u * v^2 - v * (F + k)$$

```

type of simulation: particle-mesh
Particle sets:
name particles
properties
  velocity d:3
  force d:3
Define interact in particles with self as
  p_force->force += 24.0 * 2.0 * sigma/r^7
  diff(p_force,q_force)
Define evolve in particles with self as p_
  
```

Syntax for interact, evolve, automatic insertion of interpolation, ...

S. Karol, et al. "A Domain-Specific Language and Editor for Parallel Particle Methods", In ACM TOMS'18, vol. 44, no. 3, pp. 32, Mar 2018.

N Khouzami, et al., "The OpenPME Problem Solving Environment for Numerical Simulations", In ICCS'21 pp. 614–627, Jun 2021.

Semantic gap → Debugging gap

OpenFPM library

- Modern C++ template library (for CPUs and GPUs)
- Support for dynamic load-balancing, checkpointing and communication abstractions

P. Incardona, et al "OpenFPM: A scalable open framework for particle and particle-mesh codes on parallel computers", Computer Physics Communications, 2019

Template meta-programming

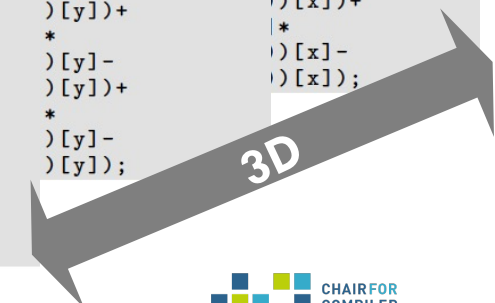
$$\frac{D\omega}{Dt} = (\omega \cdot \nabla)u + v\Delta\omega$$

What we want

What we code
(already quite abstracted!)

```

g_dwp.template get<rhs>(key)[x]=
  fac1*(g_vort.template get<vorticity>(key.move(x,1))[x]+
  g_vort.template get<vorticity>(key.move(x,-1))[x])+
  g_dwp.template get<rhs>(key)[y]=
  fac1*(g_vort.template get<vorticity>(key.move(x,1))[y]+
  g_vort.template get<vorticity>(key.move(x,-1))[y])+
  g_dwp.template get<rhs>(key)[z]=
  fac1*(g_vort.template get<vorticity>(key.move(x,1))[z]+
  g_vort.template get<vorticity>(key.move(x,-1))[z])+
  fac2*(g_vort.template get<vorticity>(key.move(y,1))[z]+
  g_vort.template get<vorticity>(key.move(y,-1))[z])+
  fac3*(g_vort.template get<vorticity>(key.move(z,1))[z]+
  g_vort.template get<vorticity>(key.move(z,-1))[z])-
  2.0f*(fac1+fac2+fac3)*
  g_vort.template get<vorticity>(key)[z]+
  fac4*g_vort.template get<vorticity>(key)[x]*
  (g_vel.template get<velocity>(key.move(x,1))[z]-
  g_vel.template get<velocity>(key.move(x,-1))[z])+
  fac5*g_vort.template get<vorticity>(key)[y]*
  (g_vel.template get<velocity>(key.move(y,1))[z]-
  g_vel.template get<velocity>(key.move(y,-1))[z])+
  fac6*g_vort.template get<vorticity>(key)[z]*
  (g_vel.template get<velocity>(key.move(z,1))[z]-
  g_vel.template get<velocity>(key.move(z,-1))[z]);
  
```



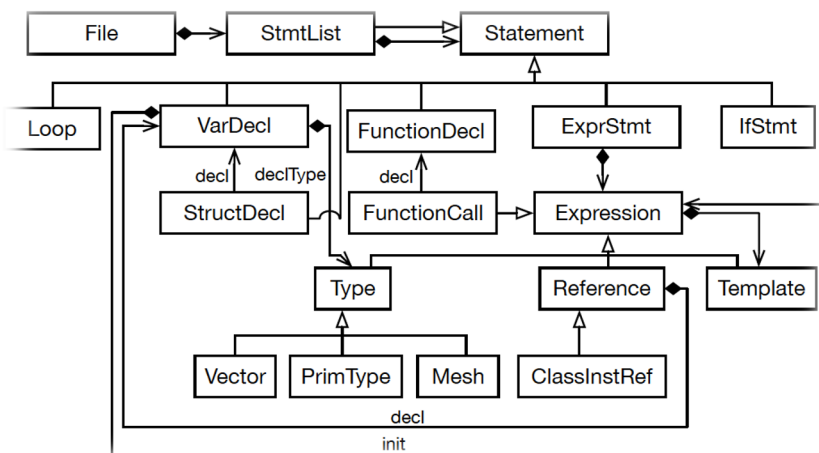
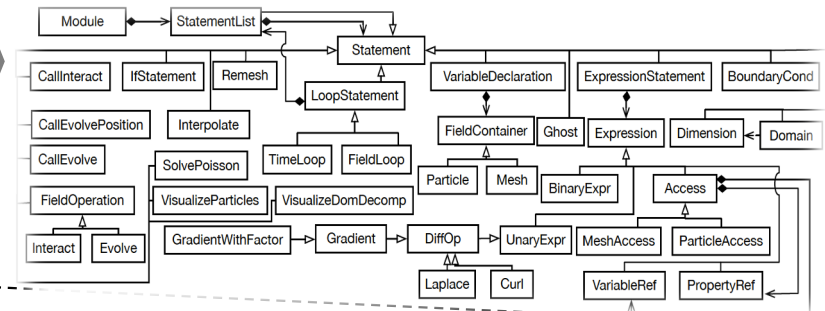
Model-to-model code generation

OpenPME DSL

```
rhs -> vortex_stretching_m =
(vorticity_mesh -> vorticity_m.v)
velocity_mesh -> velocity_m +
nu * Δ vorticity_mesh -> vorticity_m
```

Intermediate representation (IR)

```
for mesh node decl <no type> loopNodeM in rhs
loopNodeM -> vortex_stretching_m [ 0 ] = ...
loopNodeM -> vortex_stretching_m [ 1 ] = ...
loopNodeM -> vortex_stretching_m [ 2 ] = ...
```



```
while (mloop_iterator_h5a0.isNext())
{
  g_dwp.template get<rhs>(key)[x]=
  fac1*(g_vort.template get<vorticity>(key.move(x,1))[x]+
  g_vort.template get<vorticity>(key.move(x,-1))[x])+
  fac2*(g_vort.template get<vorticity>(key.move(y,1))[x]+
  g_vort.template get<vorticity>(key.move(y,-1))[x])+
  fac3*(g_vort.template get<vorticity>(key.move(z,1))[x]+
  g_vort.template get<vorticity>(key.move(z,-1))[x]) -
  2.0f*(fac1+fac2+fac3)*
  g_vort.template get<vorticity>(key)[x]+
  fac4*g_vort.template get<vorticity>(key)[x]*
  (g_vel.template get<velocity>(key.move(x,1))[x]-
  g_vel.template get<velocity>(key.move(x,-1))[x])+
  fac5*g_vort.template get<vorticity>(key)[y]*
  (g_vel.template get<velocity>(key.move(y,1))[x]-
  g_vel.template get<velocity>(key.move(y,-1))[x])+
  fac6*g_vort.template get<vorticity>(key)[z]*
  (g_vel.template get<velocity>(key.move(z,1))[x]-
  g_vel.template get<velocity>(key.move(z,-1))[x]);
  g_dwp.template get<rhs>(key)[y]=
  g_dwp.template get<rhs>(key)[z]=
}
```

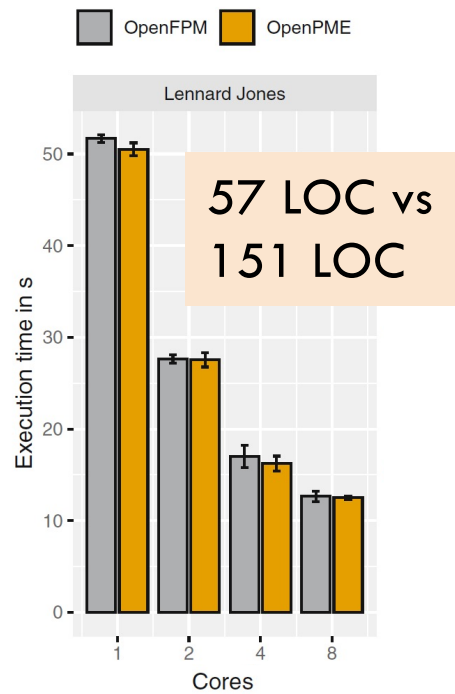
N Khouzami, et al., "The OpenPME Problem Solving Environment for Numerical Simulations", In ICCS'21 pp. 614–627, Jun 2021

OpenFPM

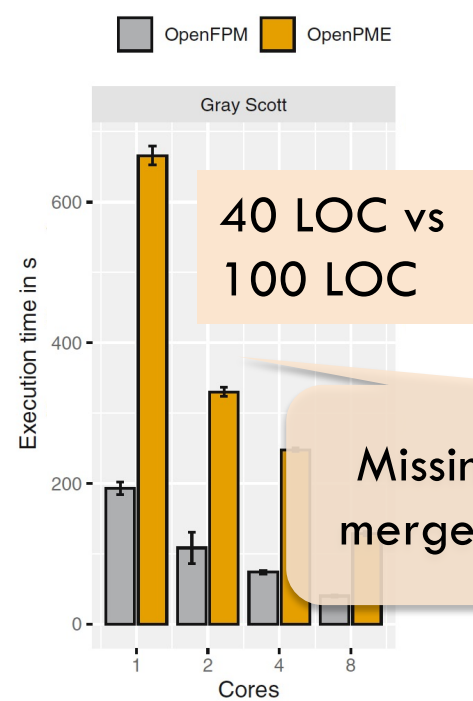
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Closing the performance gap

Lennard Jones
(particles, discrete)

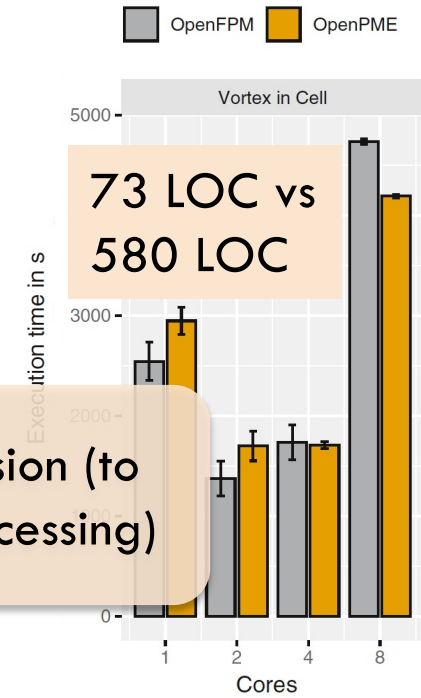


Gray-Scott
(mesh, continuous)



Missing loop fusion (to merge mesh processing)

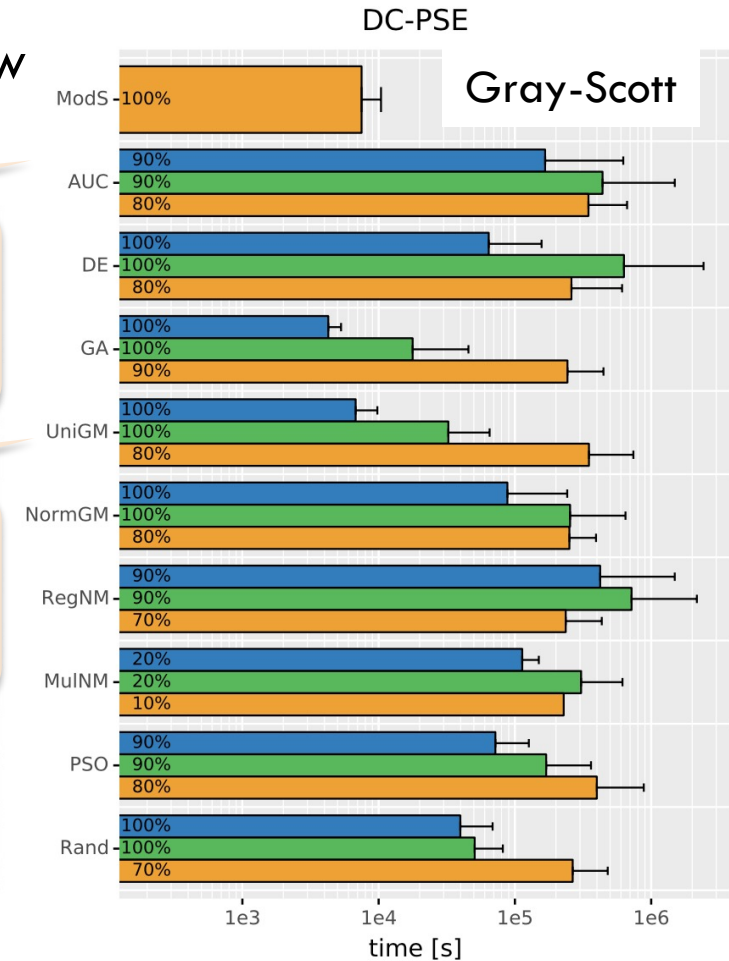
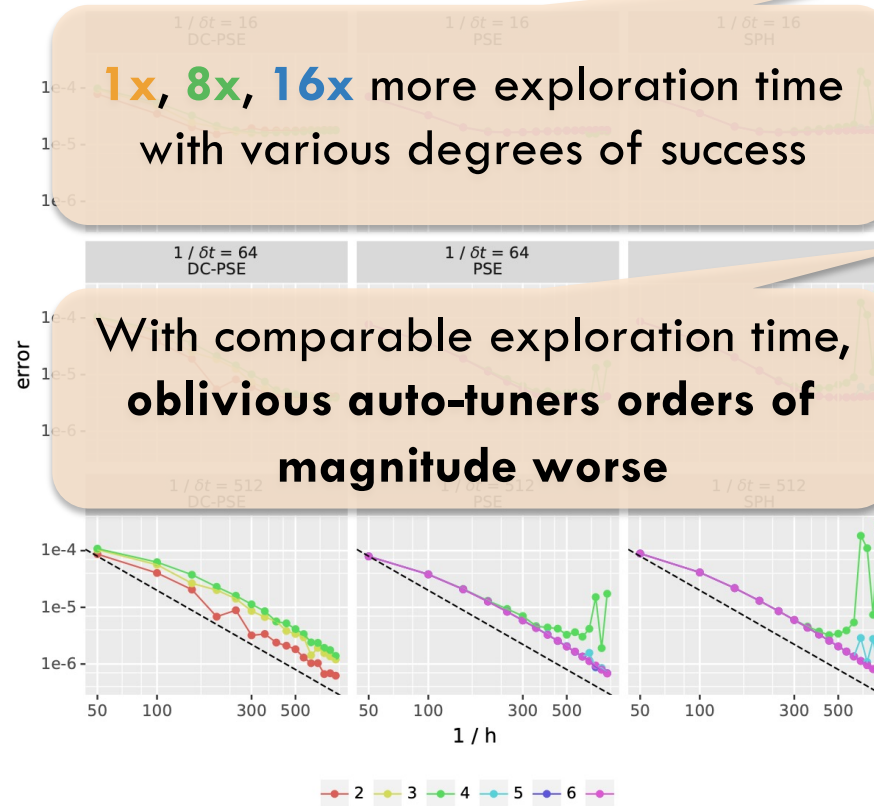
Vortex in Cell
(hybrid, continuous)



N Khouzami, et al., "The OpenPME Problem Solving Environment for Numerical Simulations", In ICCS'21 pp. 614–627, Jun 2021

Higher-level optimizations

- ❑ Insertion of ghost-gets, based on high-level dataflow
- ❑ Model-based auto-tuning for discretization
- ❑ Theoretical convergence to steer search



Formal language – added value

- Mathematical expressions: Possible to explore performance-accuracy trade-offs
- Type system: High-level semantics checks (e.g., units)

$$\begin{array}{c}
 \text{VAR} \frac{\Gamma(v) = \tau}{\Gamma \vdash v : \tau} \quad \text{VARDECL} \frac{}{\Gamma \vdash \tau x : \Gamma \cup \{x = \tau\}} \quad \text{VARINIT} \frac{\Gamma \vdash e : \tau' \quad \tau' \leq \tau}{\Gamma \vdash \tau x = e : \Gamma \cup \{x = \tau\}} \\
 \\
 \text{PAREN} \frac{\Gamma \vdash e : \tau}{\Gamma \vdash (e) : \tau} \quad \text{ASSIGN} \frac{\Gamma \vdash x : \tau \quad \Gamma \vdash e : \tau' \quad \tau' \leq \tau}{\Gamma \vdash x = e : \tau} \\
 \\
 \text{VECAACC} \frac{\Gamma \vdash v : \mathbb{V}\langle\tau\rangle \quad \Gamma \vdash i : \mathbb{Z} \quad i \geq 0}{\Gamma \vdash v[i] : \tau} \quad \text{MATAACC} \frac{\Gamma \vdash m : \mathbb{M}\langle\tau\rangle \quad \Gamma \vdash i, j : \mathbb{Z} \quad i, j \geq 0}{\Gamma \vdash m[i][j] : \tau} \\
 \\
 \text{PARTSCAACC} \frac{\Gamma \vdash p : \mathbb{P} \quad \Gamma \vdash f : \mathcal{E}\langle\tau, 1\rangle}{\Gamma \vdash p \rightarrow f : \tau} \quad \text{PARTVECAACC} \frac{\Gamma \vdash p : \mathbb{P} \quad \Gamma \vdash f : \mathcal{E}\langle\tau, n\rangle, n \geq 2}{\Gamma \vdash p \rightarrow f : \mathbb{V}\langle\tau\rangle} \\
 \\
 \text{UNARY} \frac{\Gamma \vdash e : \tau \quad \tau_{\Theta}(\tau) \neq \perp}{\Gamma \vdash \Theta e : \tau_{\Theta}(\tau)} \quad \text{BINLOG} \frac{\Gamma \vdash e_1 : \mathbb{B} \quad \Gamma \vdash e_2 : \mathbb{B}}{\Gamma \vdash e_1 \otimes_{\log} e_2 : \mathbb{B}} \\
 \\
 \text{BINREL} \frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_{\otimes}(\tau_1, \tau_2) \neq \perp}{\Gamma \vdash e_1 \otimes_{\text{rel}} e_2 : \mathbb{B}} \quad \text{BINARI} \frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_{\otimes}(\tau_1, \tau_2) \neq \perp}{\Gamma \vdash e_1 \otimes_{\text{arith}} e_2 : \tau_{\otimes}(\tau_1, \tau_2)} \\
 \\
 \text{ERRUNARY} \frac{\Gamma \vdash e : \tau \quad \tau_{\Theta}(\tau) = \perp}{\Gamma \vdash \Theta(e) : \mathbb{E}} \quad \text{ERRBIN} \frac{\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \quad \tau_{\otimes}(\tau_1, \tau_2) = \perp}{\Gamma \vdash e_1 \otimes e_2 : \mathbb{E}}
 \end{array}$$

S. Karol, et al. "A Domain-Specific Language and Editor for Parallel Particle Methods", In ACM TOMS'18, vol. 44, no. 3, pp. 32, Mar 2018.

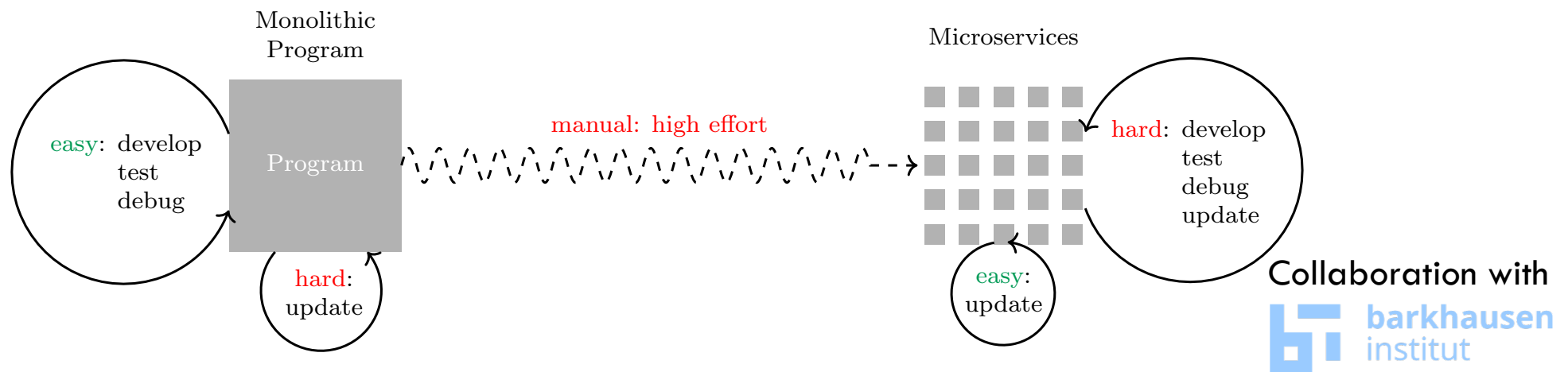
$\Theta \in \{-, !, \sqrt{\quad}\}$, $\otimes_{\text{arith}} \in \{+, -, *, /, a^b\}$, $\otimes_{\log} \in \{\&\&, ||\}$, $\otimes_{\text{rel}} \in \{==, !=, <, >, <=, >=\}$
 $\mathbb{Z} = \text{Integer}$, $\mathbb{R} = \text{Real}$, $\mathbb{P} = \text{Particle}$, $\mathbb{V} = \text{Vector}$, $\mathbb{M} = \text{Matrix}$, $\mathcal{E} = \text{Field/Property}$, $\mathbb{E} = \text{Error}$

Examples (3): Big data (only briefly)

- Dataflow IR from a sequential syntax (Rust or Java-like)

```
let v1_1_0 = join(customer, sales, cc_sk, c_sk);
let v1_1 = join(v1_1_0, date_dim, sd_sk, d_d_sk);
let gs = group_by(v1_1, gb_key);
let mut v1 = Vec::new();
for group in gs {
    let result = compute(group, sale_type);
    v1.push(result);
}
```

Sequential code (implicit parallelism)

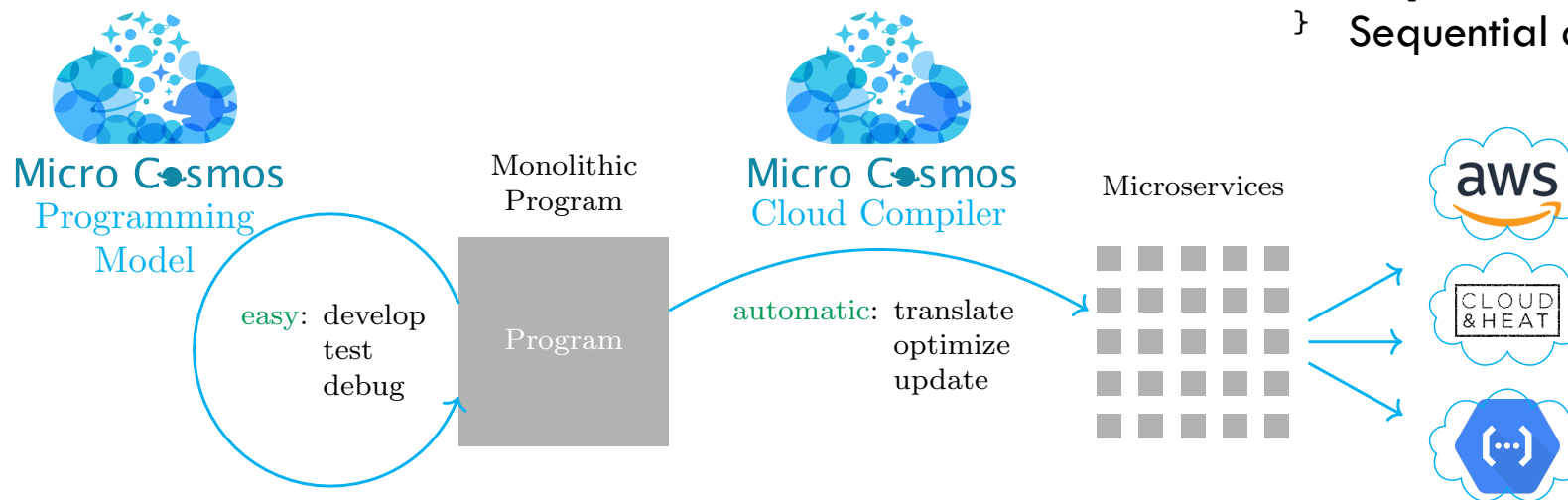


Examples (3): Big data (only briefly)

- ❑ Dataflow IR from a sequential syntax (Rust or Java-like)
- ❑ IR to abstract from “cloud ISAs”

```
let v1_1_0 = join(customer, sales, cc_sk, c_sk);
let v1_1 = join(v1_1_0, date_dim, sd_sk, d_d_sk);
let gs = group_by(v1_1, gb_key);
let mut v1 = Vec::new();
for group in gs {
    let result = compute(group, sale_type);
    v1.push(result);
}
```

Sequential code (implicit parallelism)



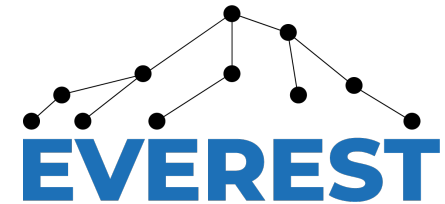
S. Ertel, A. Goens, J. Adam, J. Castrillon, "Compiling for Concise Code and Efficient I/O", Proceedings of the 27th International Conference on Compiler Construction (CC 2018), ACM, pp. 104–115,

Collaboration with

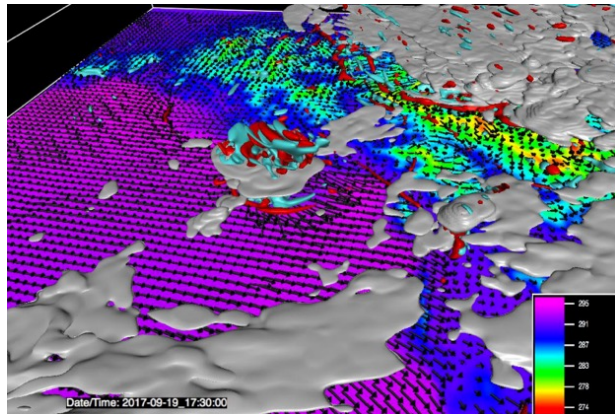


EVEREST: Efficient large-scale heterogeneous computing

- ❑ Current work on large-scale EU H2020 project Everest
 - ❑ Stencil and Tensor Operations in Weather Modelling (WRF)
 - ❑ Interplay orchestration (dataflow) and kernels
 - ❑ MLIR framework for reusable abstractions

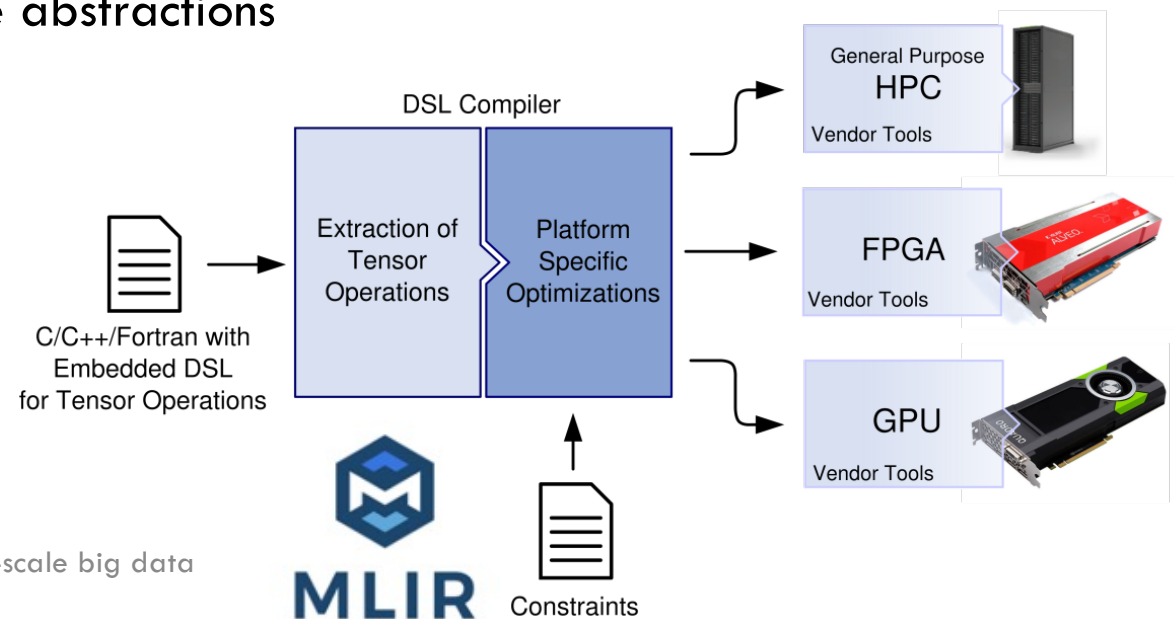


<https://everest-h2020.eu>



CIMA Foundation

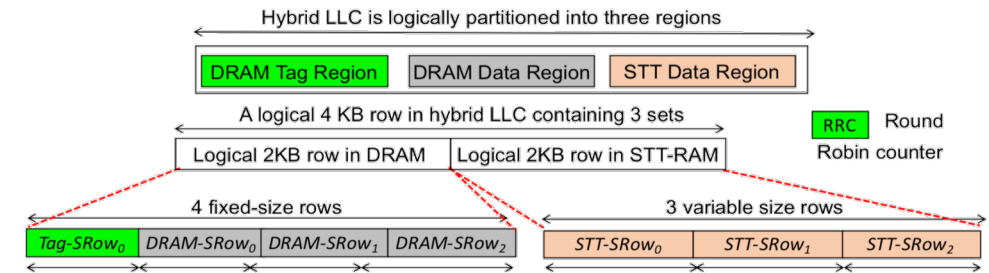
C. Pilato, et al. "EVEREST: A design environment for extreme-scale big data analytics on heterogeneous platforms", DATE 2021



Challenges ahead: Emerging memories

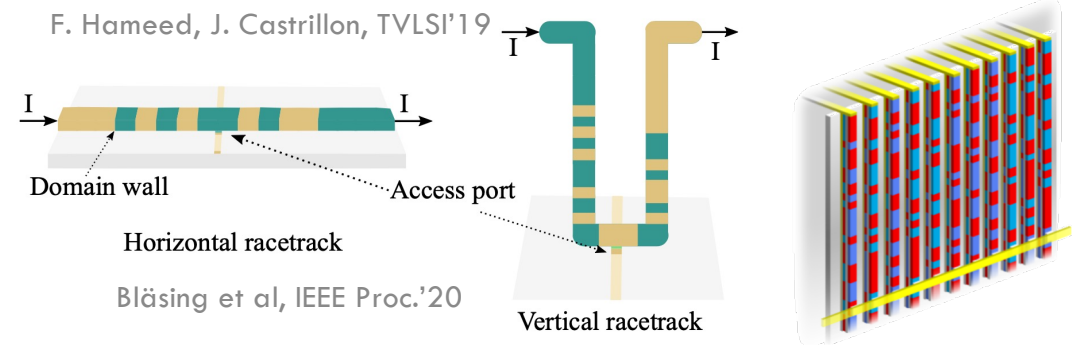
Example: Hybrid STT-/DRAM

- Placement and layout optimization
- Hints for memory controllers



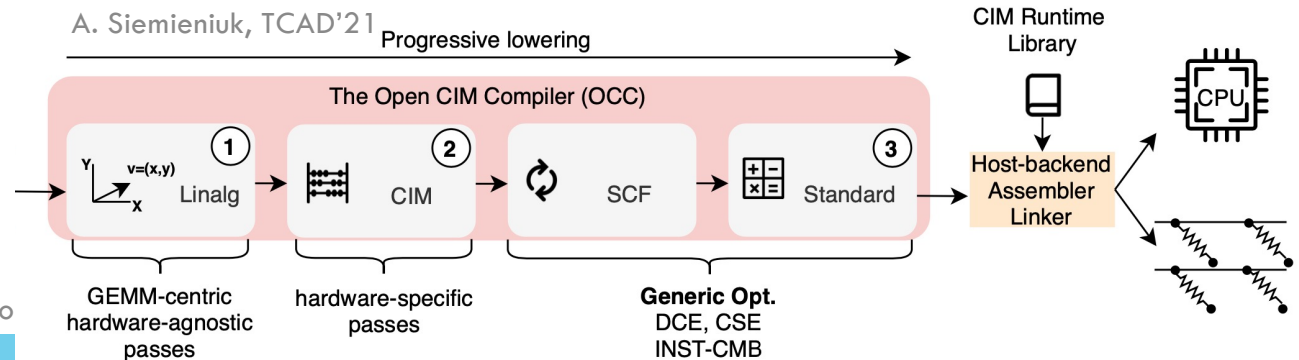
Racetrack memories

- Extreme density
- Sequential bit access per cell



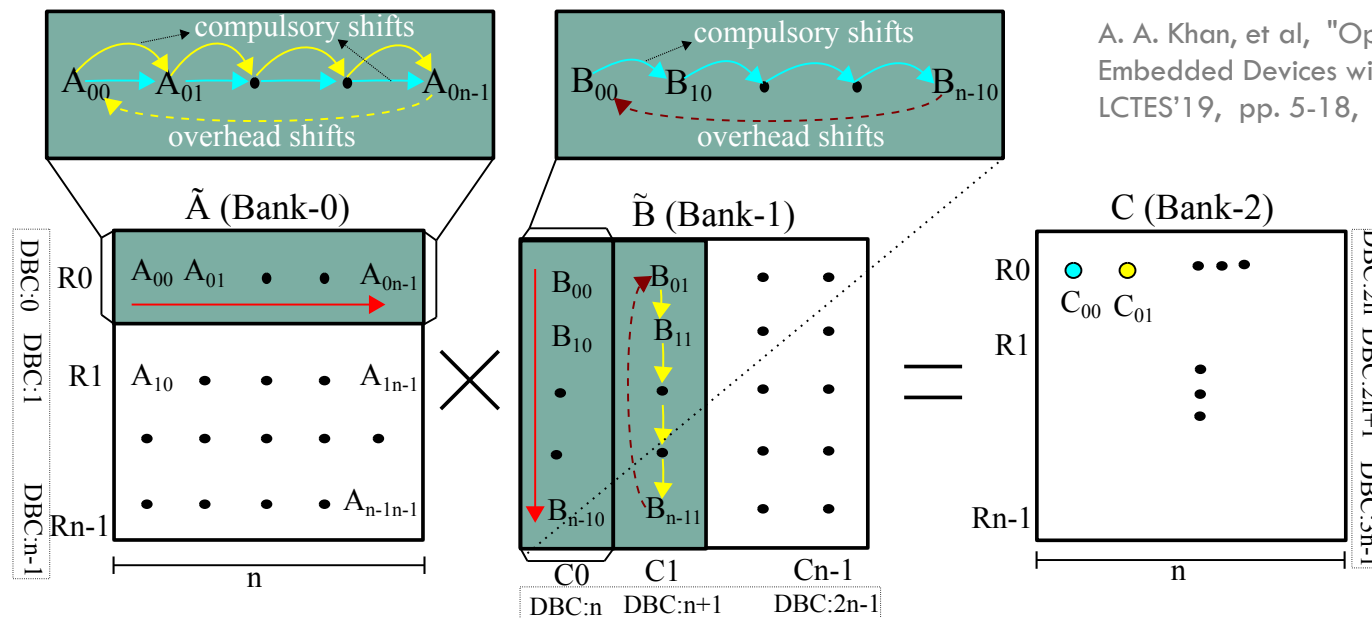
Memristive accelerators

- In-memory computing
- Compiler abstractions



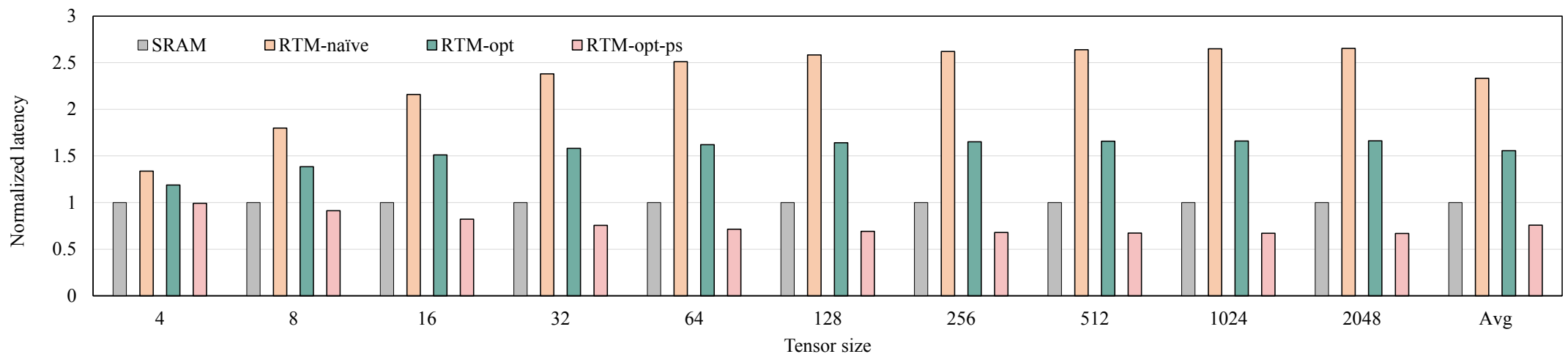
Architecture and data layout optimization

- Underlying idea: Zig-zag through data to reduce number of shifts
 - Exploit explicit patterns in high-level DSLs
 - Recognize patterns with polyhedral compilers



Latency comparison vs SRAM

- ❑ Un-optimized and naïve mapping: Even worse latency than SRAM
- ❑ 24% average improvement (even with very conservative circuit simulation)

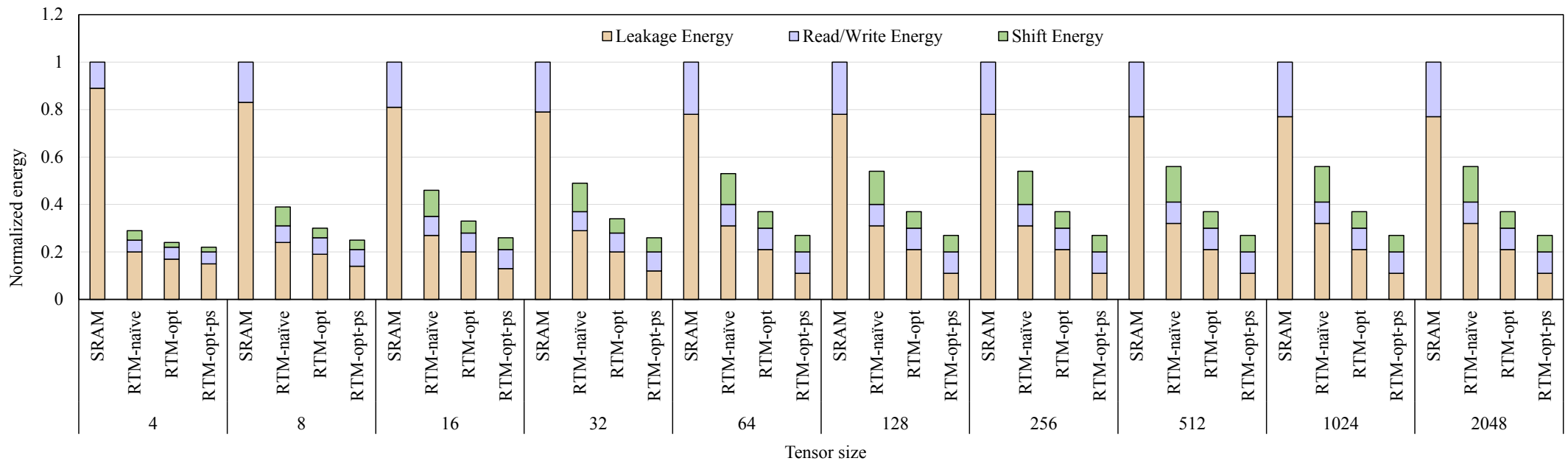


A. A. Khan, et al, "Optimizing Tensor Contractions for Embedded Devices with Racetrack Memory Scratch-Pads", LCTES'19, pp. 5-18, 2019

A. A. Khan, et al. "Optimizing Tensor Contractions for Embedded Devices with Racetrack and DRAM Memories". ACM TECS 2020

Energy comparison vs SRAM

- Higher savings due to less leakage power
- 74% average improvement (in addition to savings due to DRAM placement)

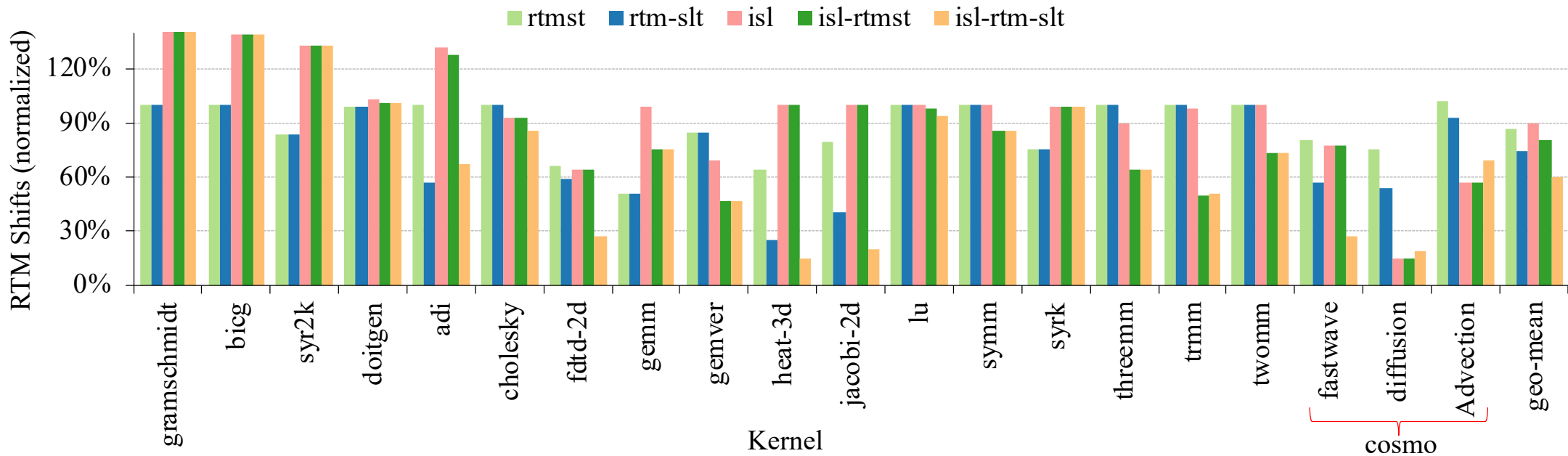


A. A. Khan, et al, "Optimizing Tensor Contractions for Embedded Devices with Racetrack Memory Scratch-Pads", LCTES'19, pp. 5-18, 2019

A. A. Khan, et al. "Optimizing Tensor Contractions for Embedded Devices with Racetrack and DRAM Memories". ACM TECS 2020

Generalization to stencils and other kernels

- Average improvements in performance (~20%) and energy consumption (~40%)



A. A. Khan, et al., "Polyhedral Compilation for Racetrack Memories", In IEEE TCAD'20, vol. 39, no. 11, pp. 3968-3980, Oct 2020.

Summary

- ❑ Tame ever-increasing system complexity
 - ❑ Still highly-relevant optimizing compilers (polyhedral, ...)
 - ❑ DSL examples: expose higher semantics (efficiency, productivity)
 - ❑ Higher semantics key for emerging accelerators/systems!

- ❑ Moving forward
 - ❑ Semantic-preserving transformations
 - ❑ Larger use cases (e.g., WRF in the context of EVEREST)
 - ❑ Common abstraction across novel paradigms (e.g., as MLIR dialects across in-memory computing architectures)

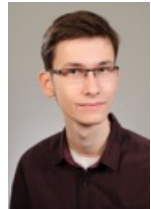
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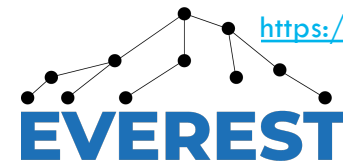


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Wittwer

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<https://everest-h2020.eu>

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Parkin, P. Jääskeläinen)

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